

# Reef

**Fast Succinct Non-Interactive Zero-Knowledge  
Regex Proofs**



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# Scenario - Clinical Trials

Patty registers online for Vikki's clinical trial and is automatically accepted

Patty



Vikki



.\*ACTG...

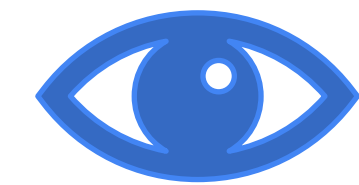


Vikki can't ensure Patty actually qualifies

# Have Patty send her DNA

Patty can send Vikki her DNA to verify

Patty



Vikki



.\*ACTG...



Vikki has Patty's DNA in plain text, even if Patty isn't accepted into the trial

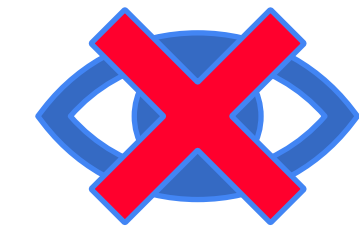
**We want to prove Patty qualifies for  
Vikki's trial**

**Without Vikki learning Patty's DNA before  
she's enrolled**

# Zero Knowledge Proofs

Patty can register for Vikki's trial and attach a **proof** that she qualifies

Patty



Vikki



.\*ACTG...



Vikki only learns if Patty qualifies for her trial

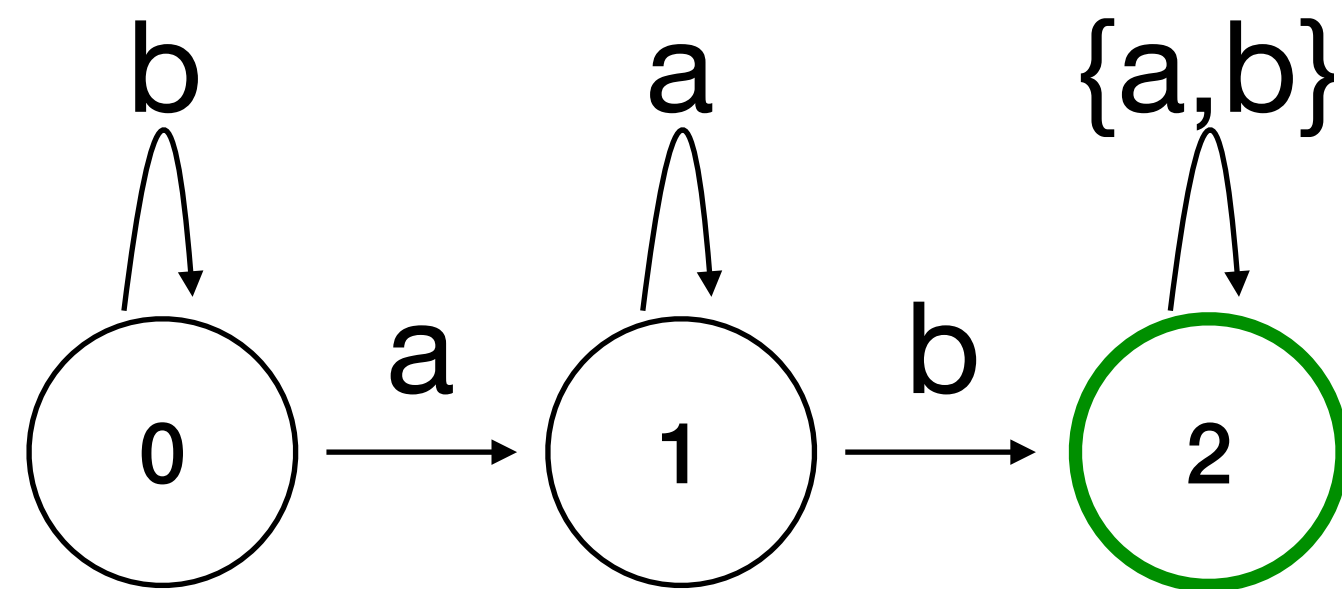
# How to make a ZKP in 4 easy steps...

1. Vikki expresses her regex matching statement as a circuit satisfiability instance
2. Vikki publishes her circuit
3. Patty finds a satisfying witness
4. Patty proves to Vikki that she knows the satisfying witness

# Naive Solution

$a+b \cdot *$

(Q: {0,1,2},  $\Sigma$ : {a,b},  $\delta$ ,  $q_0$ :{0}, F:{2})



Limited Expressivity



```
field match(field commit, field blind) {  
    field[SIZE] document = open(commit,  
                                blind);  
  
    field state = 0; // initial state  
    for (i = 0; i < SIZE; i++) {  
        state = delta(state, document[i]);  
    }  
  
    if (state == 2) { // accepting state  
        return 1; // match  
    } else {  
        return 0; // no match  
    }  
}
```

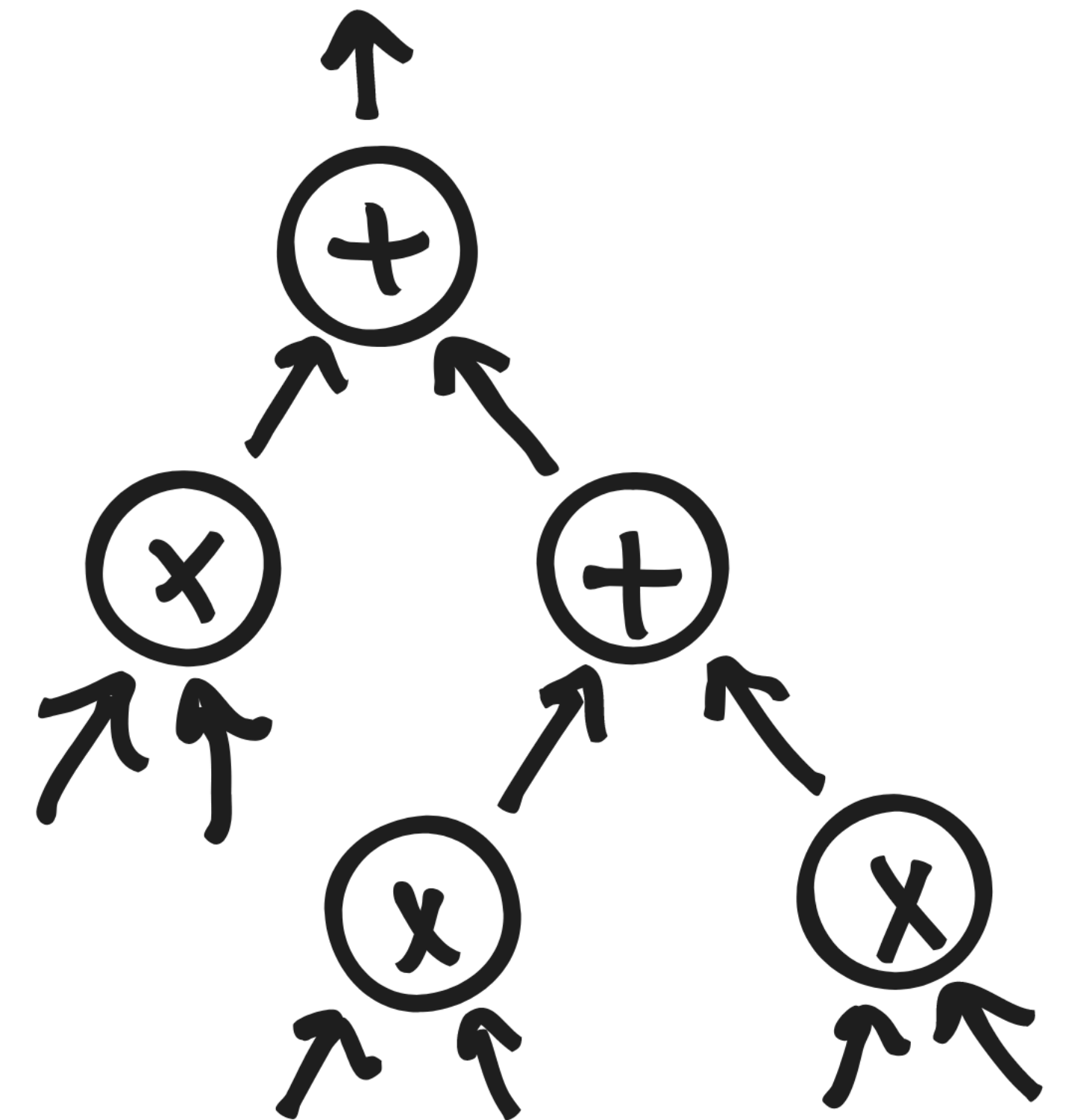


# Going from match to circuit

```
field delta(field state, field cur_char) {  
  if (state == 0 && cur_char == 0) return 1;  
  if (state == 0 && cur_char == 1) return 0;  
  ...  
  if (state == 2 && cur_char == 1) return 2;  
  return -1; // invalid state or character  
}
```



Unfold delta |document| times





# Key Insight 1 - Skipping Alternating Finite Automata

Alternating Finite Automata give us greater **expressivity**

We can extend AFA to **skip** irrelevant parts of the document

# Key Insight 2 - Lookup Arguments

We can represent the cascading `if` statements as (start state, character, end state) lookup arguments in the circuit

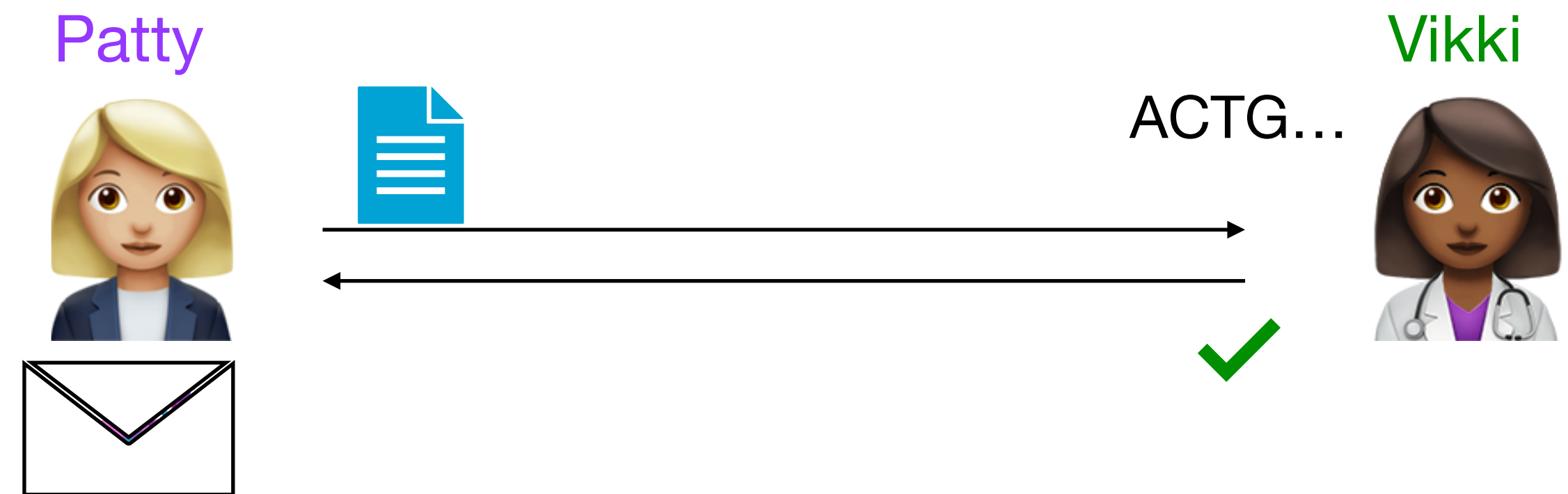
# Key Insight 3 - Recursion

We can make iterating through the document much faster using a  
recursive proof system

**Reef is able to decouple Prover running time from document size**

# Reef - Zero Knowledge Regex Proofs

- **Patty commits** to her DNA
- **Vikki publishes** a regex of the genetic variant required to participate in her trial
- **Patty proves (in zero knowledge)** that her committed DNA matches the public regex
- **Vikki verifies** Patty's proof



# Roadmap

→ Background

Reef

Skipping Alternating Finite Automata

Lookup Arguments

Adding Recursion

Optimizations

Evaluation

Future Work

Summary

# Background - Zero Knowledge Proofs

- Protocol that allows a Prover  $P$  to prove some statement to a Verifier  $V$
- Proofs are...
  - **Complete** -  $V$  is always convinced of a true statement
  - **Sound** -  $P$  cannot convince  $V$  of a false statement
  - **Zero Knowledge** -  $V$  learns nothing except the truth of the statement
- Proofs are arithmetized using **rank-1 constraint satisfiability (R1CS)**
  - 1 constraint = 1 multiplication in circuit
  - More constraints  $\rightarrow$  more complex proof



# Background - Recursive Proof Systems

- Produce a proof  $\pi$  for each `do x`

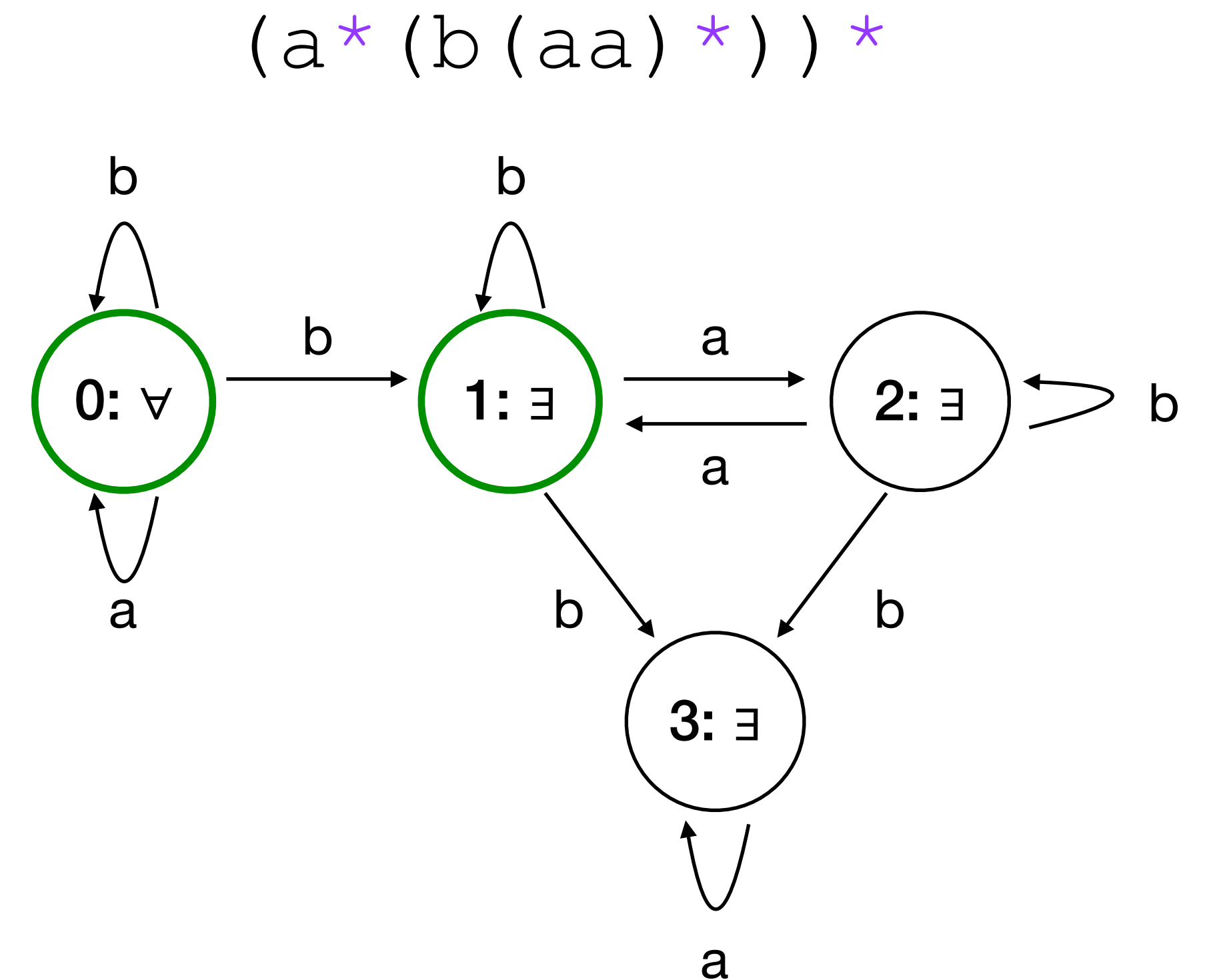
```
for (i = 0; i < j; i++) {  
    do x;  
}
```

$$\pi_0 \longrightarrow \pi_{1+V(\pi_0)} \longrightarrow \dots \longrightarrow \pi_{j-1+V(\pi_{j-2})} \longrightarrow \pi_{j+V(\pi_{j-1})}$$

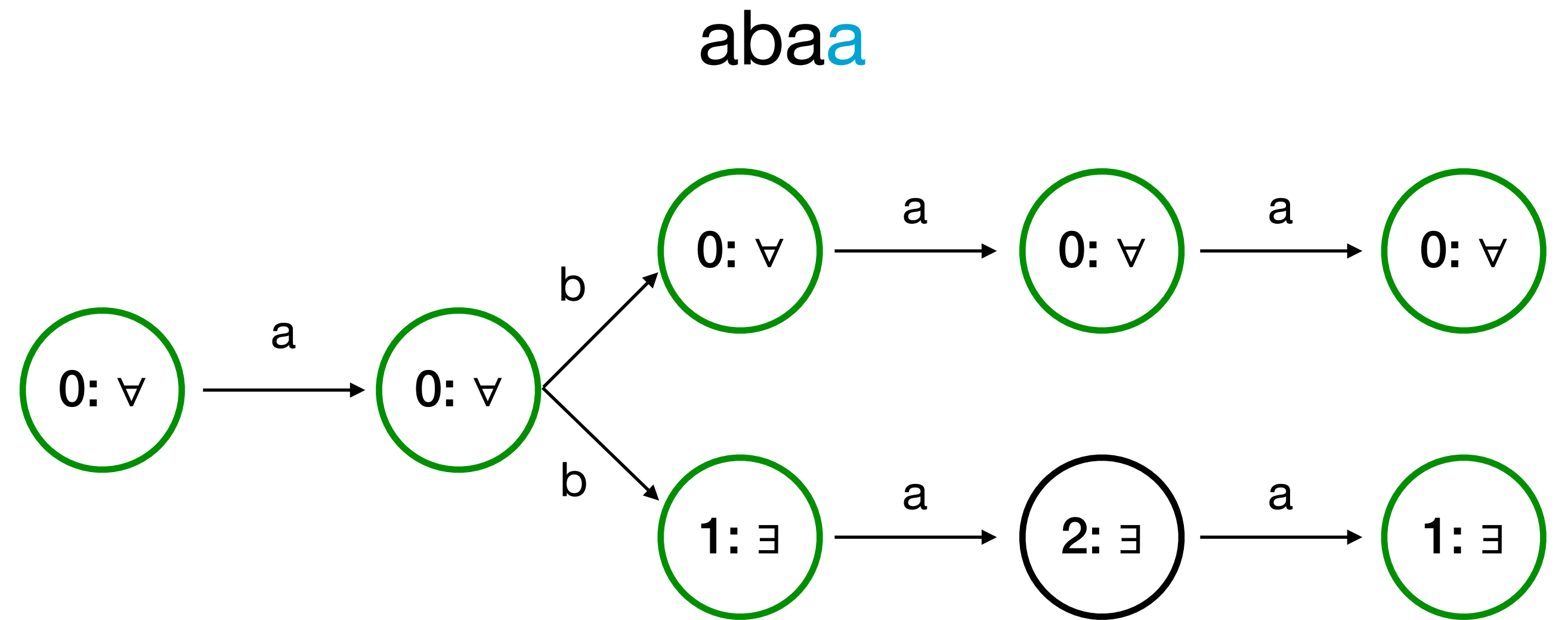
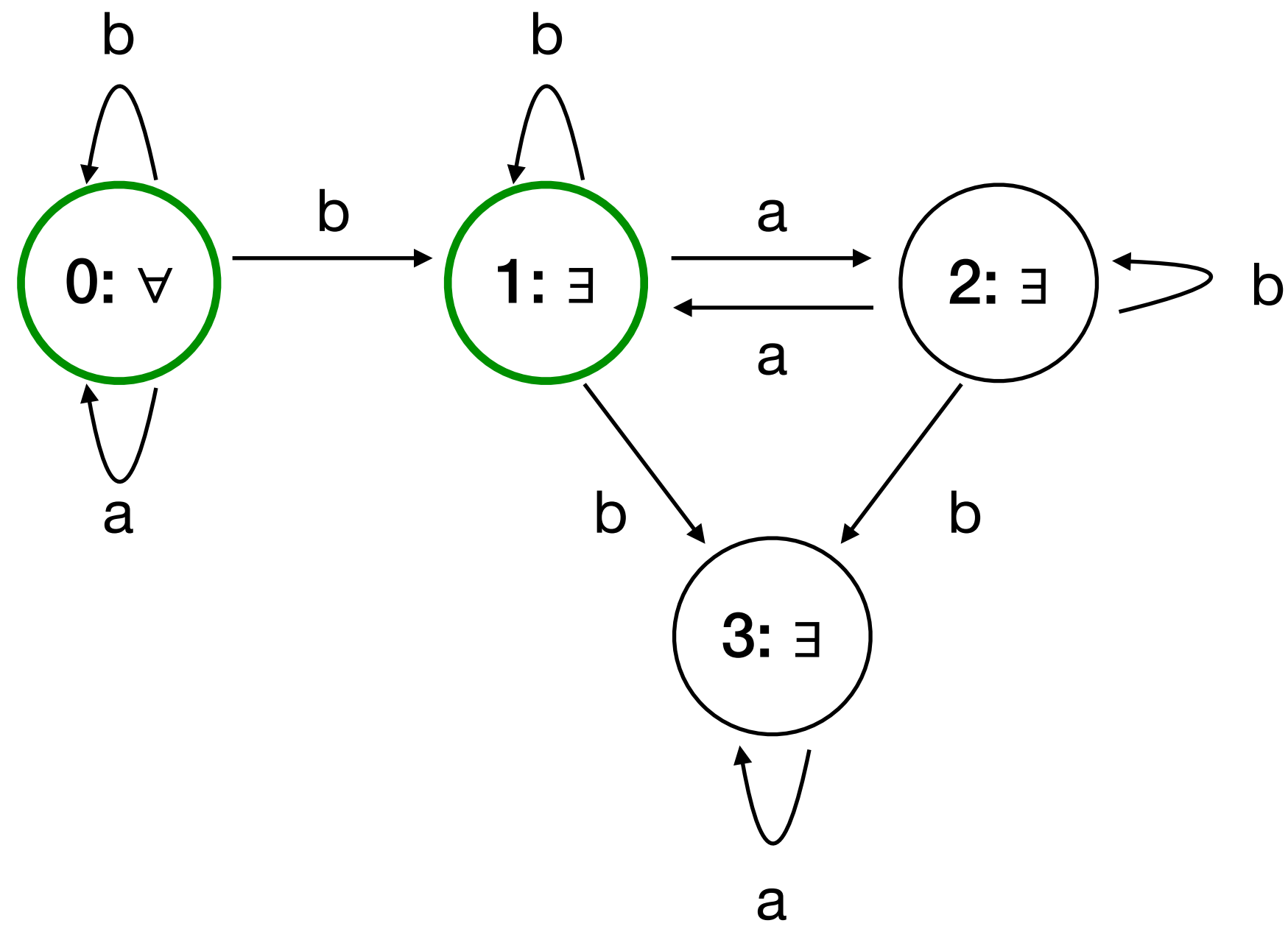
- Circuit size is parameterized by **just one iteration**

# Background - Alternating Finite Automata

- Generalization of NFA with states labeled as  $\exists$  or  $\forall$
- $\exists$  same as normal NFA
- $\forall$  takes all transitions in parallel
- All  $\forall$  transition paths must accept
- $\forall$  transitions support lookarounds



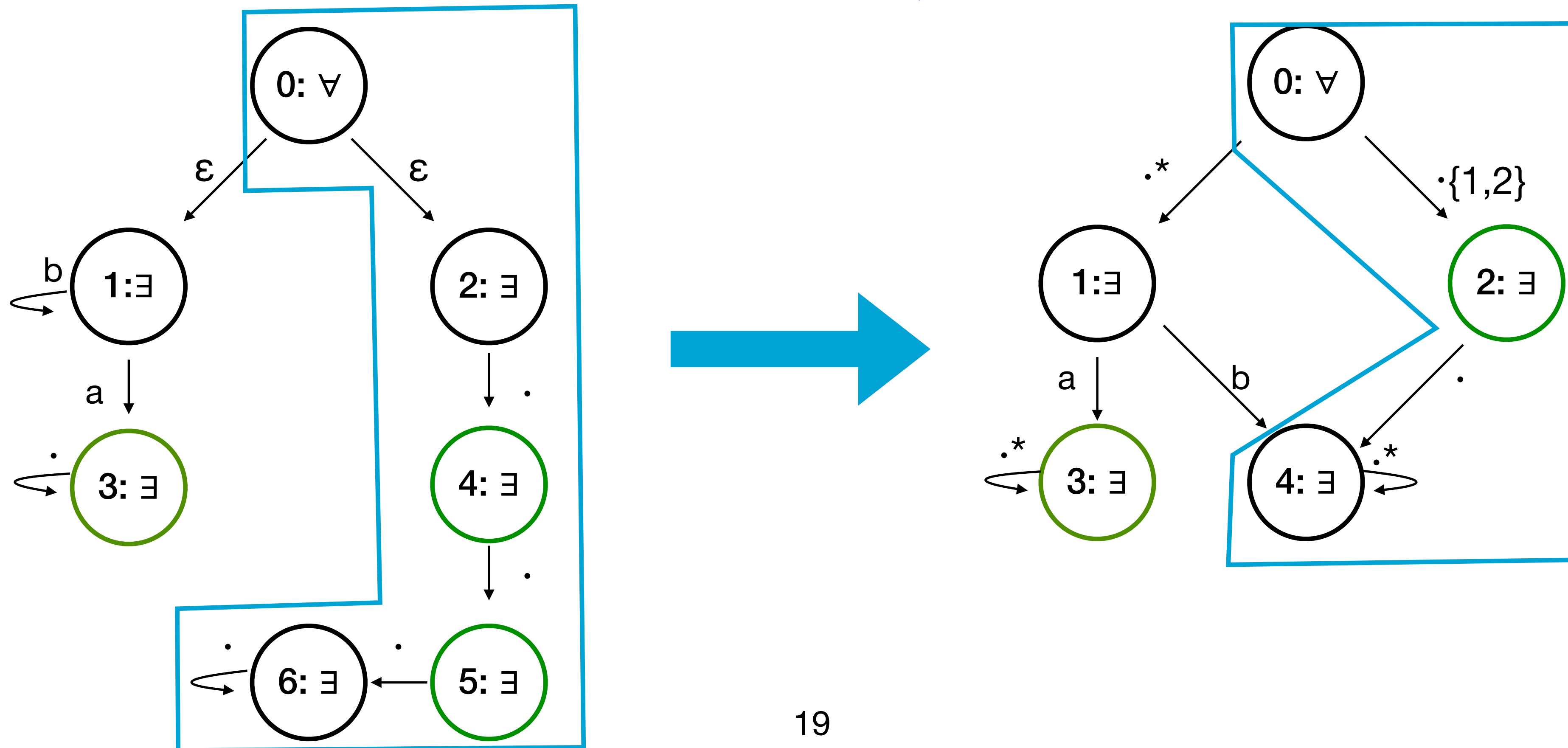
# Background - Alternating Finite Automata



# Skipping Alternating Finite Automata

- Compress multiple wildcards ( $\cdot\{n\}$ ,  $\cdot\{m,n\}$ ,  $\cdot^*$ ) into a single transition

( $? = \cdot^* a$ )  $\cdot\{1,2\}$



# SAFA

- Designed to work with NP-Checkers
  - Reef traverses the SAFA with non-deterministic hints
  - Prover provides pre and post skip cursor
  - Only need to *check* that the hints are correct
- Keep track of finished branches with a minimal stack
- But how do we represent SAFA?

# Lookup Arguments

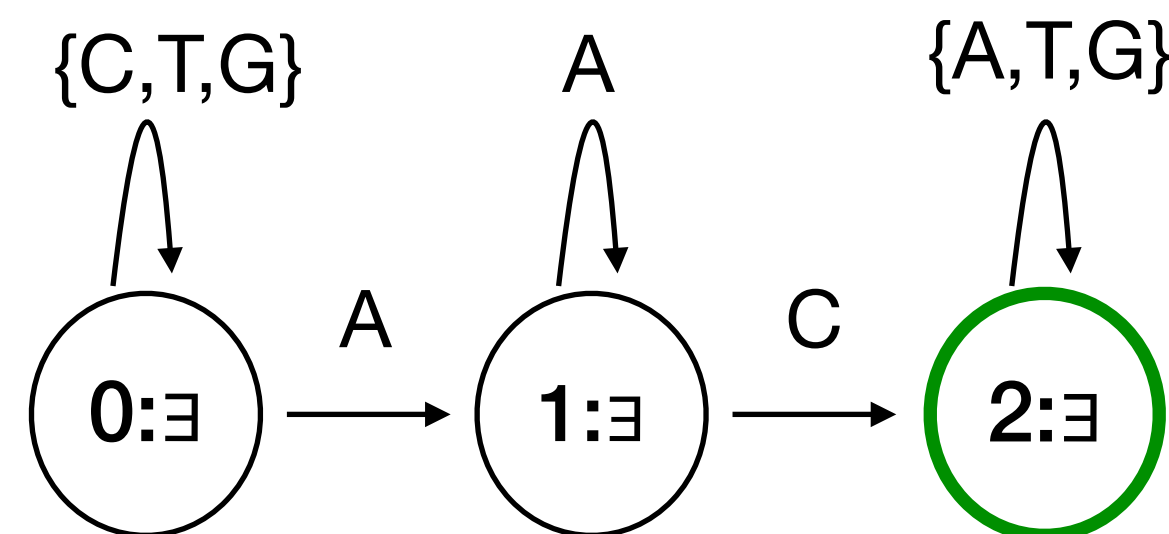
- Prove that some values  $\{v_0, \dots, v_{m-1}\}$  are in a table  $T$
- 2 tables

ACTGCTACGTC  
 GACTCTCAGACGTC  
 ACTGACGCTATATAC  
 GCGCTACGTATCAC  
 GGCACTTACAGTTA  
 ACACTGTGGGAC




0	A
1	C
2	T
3	G
...	...

Commitment - ties characters to indices



0	G	0
0	T	0
0	C	0
0	A	1
...	...	...

Replaces the delta function

# Everything's Better with Recursion

- Naive lookup argument  $\rightarrow m \cdot (\log(n) + n)$
- With recursion maintain a **running claim** to check at the end
- As the number of lookups **increases**, cost-per-lookup **decreases**

$$\begin{array}{ccc} |D| \cdot (\log(|D|) + |D|) & \longrightarrow & |D| \cdot (\log(|D|)) + |D| \\ |D| \cdot (\log(|SAFA|) + |SAFA|) & & |D| \cdot (\log(|SAFA|)) + |SAFA| \end{array}$$

↑  
Check lookup  
inclusion at each  
step



# Optimizations

- Hybrid tables
  - Public SAFA Table + Private Document Table →  $m\log(|\text{Document}| \cdot |\text{SAFA}|)$  constraints
  - Single Hybrid Public/Private Table →  $m\log(|\text{Document}| + |\text{SAFA}|)$  constraints
- Document Projections
  - Run lookup over subsets of the larger document table
  - Works for regexs with prescribed offsets
    - $\cdot\{10\}abc\cdot^*$  ✓
    - $\cdot^*abc$  ✗

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# Evaluation

- Can Reef support a variety of regexs?
- Can Reef support a variety of document sizes?
- Is Reef efficient for the prover?
- Is Reef efficient for the verifier?
- How does Reef compare to existing/alternative solution?
- Do SAFA meaningfully reduce the size of the automata?
- What impact do Reef's additional optimizations have?

# Reef supports more robust Regexs

More expressivity with fewer constraints

	Fixed String Matching	Wildcards	Kleene stars	Negation	Alternation	Lookarounds	# Constraints
Reef	✓	✓	✓	✓	✓	✓	$O(\alpha \log(D + Q_{SAFA} +  \Sigma ))$
Zombie	✓	✓	✓	✓	✓		$O(D \cdot Q_{TNFA})$
ZKRegex	✓	✓	✓	✓			$O(D \cdot Q_{TNFA} \cdot \log( \Sigma ))$
zkreg	✓	✓					$O(D + Q_{AC-DFA})$

**D** - Document Size, **Q** - # Transitions in Automata, **Σ** - Alphabet, **α** - Number of lookups

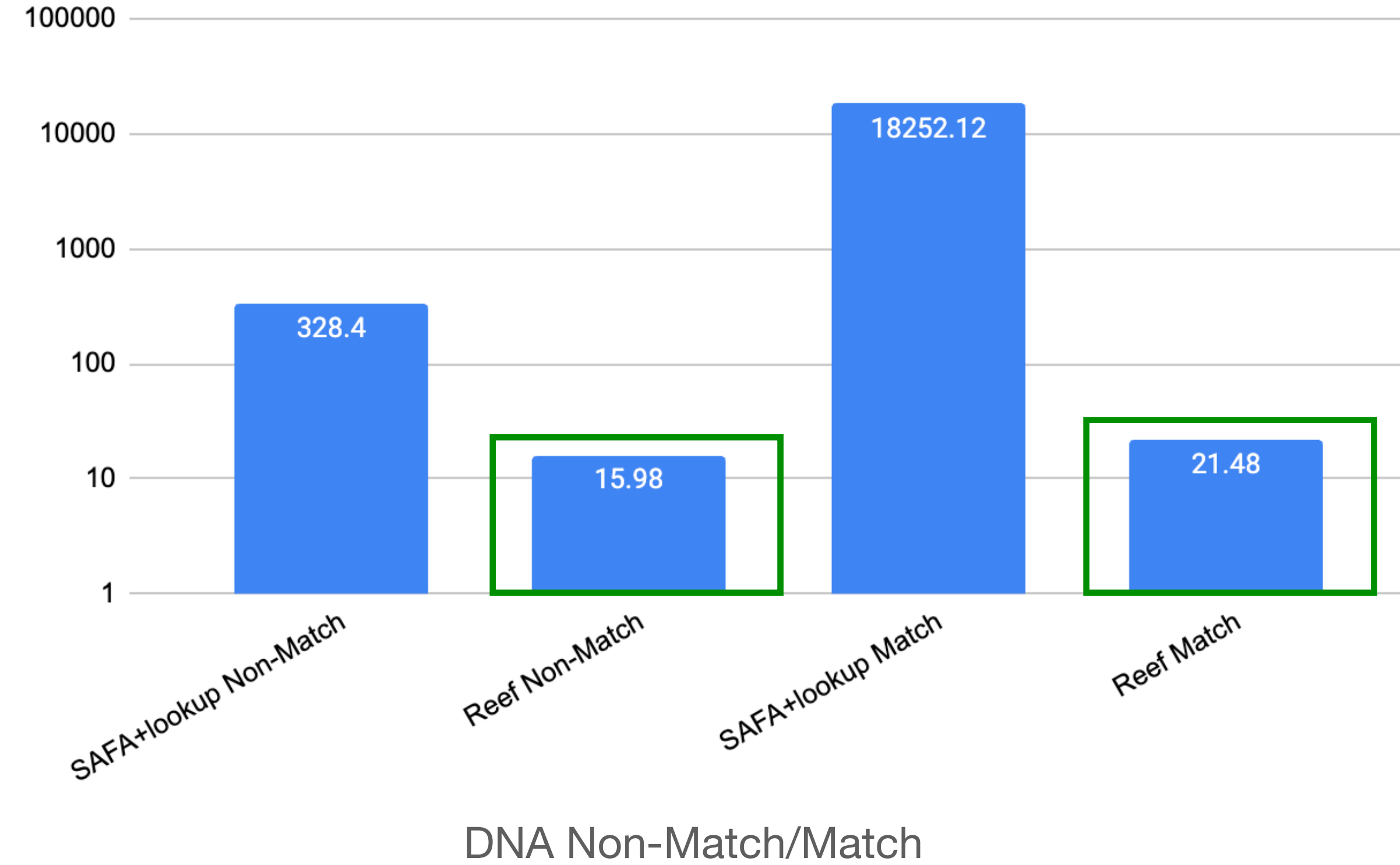
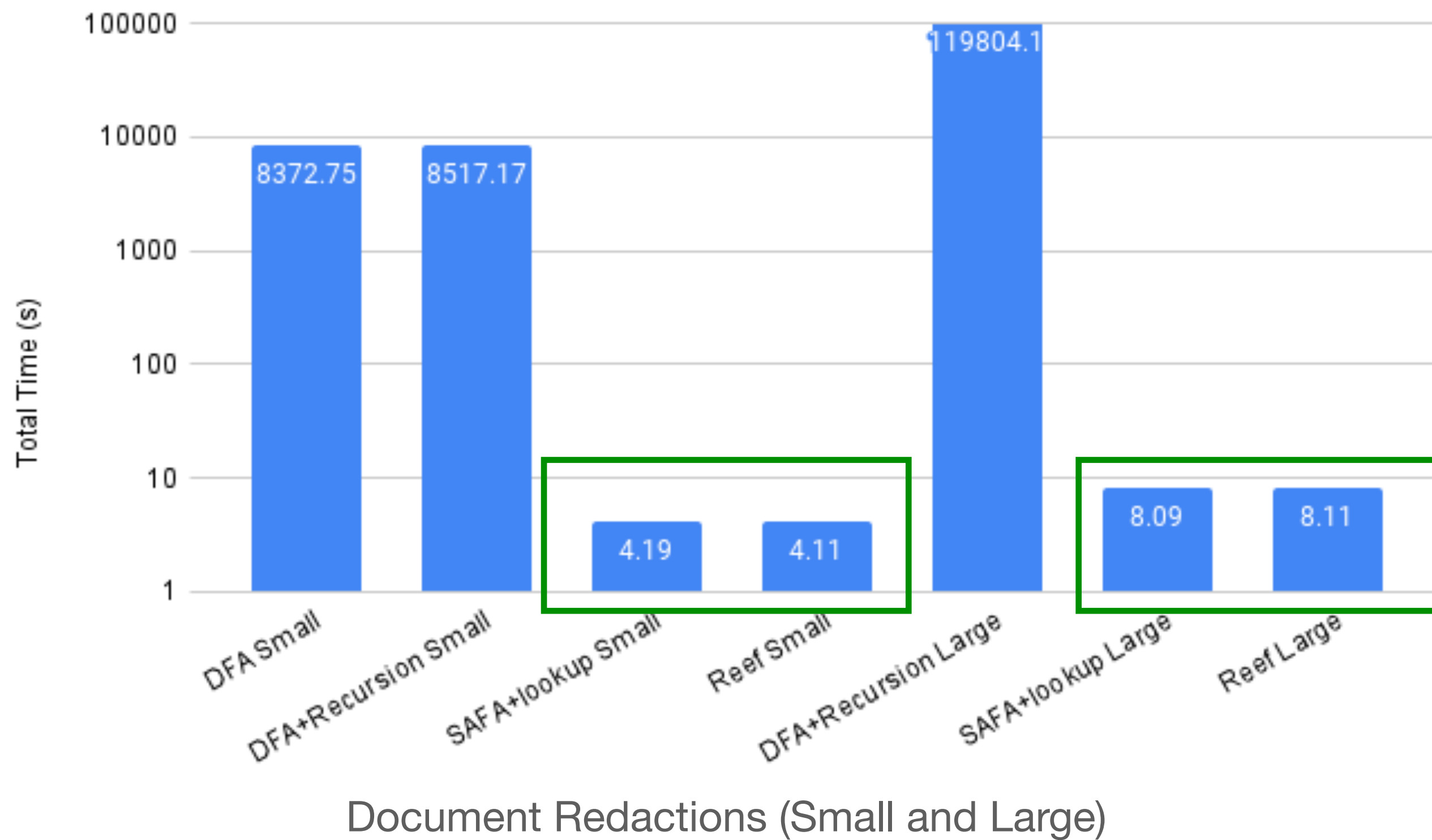
# Reef Supports a Variety of Applications

	<b>Document Size</b>	<b>Average SAFA Size - States</b>	<b>Average SAFA Size - Transitions</b>
Document Redaction (Small)	415	331	42,318
Document Redaction (Large)	1,000	908	116,751
ODoH	128	16	1,958
Strong Password Match/Non-Match	12/6-9	21	1,188
DNA Match/Non-Match	32 million - 43 million	546	29,832

# And It's More Efficient - Fewer Constraints

	DFA	DFA+Recursion	SAFA+lookup	Reef
Document Redaction (Small)	23,041,771	67,472	54,679	52,631
Document Redaction (Large)	X	141,712	57,628	54,636
ODoH	1,552,754	24,131	22,573	18,437
Password Match/Non-Match	X	X	21,002/21,721	19,982/20,725
DNA Match/Non-Match	X	X	96,296/107,184	85,352/95,916

# And It's More Efficient - Faster Total Prover Time



Even without Reef's additional optimizations, SAFA+lookup is orders of magnitude faster



# Future Work

- Extending Reef to Context Free Grammars
  - JSON Validation
- Malware detection via YARA rules
  - Static Analysis = Regex + Propositional Logic
  - How to scale to checking hundreds of regexs at once?
- Zero Knowledge Proof of Compilation
  - Use Reef for parsing phase

# Summary

Thank you!

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## We want...

- Succinct Zero Knowledge Proofs
- For a variety of regexs
- That scale well for large documents

## We can...

- Use SAFA to get better expressivity
- And skip irrelevant parts of the document
- Use lookup tables for document commitment and SAFA transitions

## Reef!

- Support for a variety of applications
- Fast Prover and Verifier times
- Fewer constraints